Enrolment No.

GUJARAT TECHNOLOGICAL UNIVERSITY BE - SEMESTER- III(NEW) EXAMINATION - WINTER 2022 Date:27-02-2023

Subject Code:3130905 Subject Name: Control System Theory Time:02:30 PM TO 05:00 PM

Total Marks:70

Instructions:

- 1. Attempt all questions.
- 2. Make suitable assumptions wherever necessary.
- 3. Figures to the right indicate full marks.
- 4. Simple and non-programmable scientific calculators are allowed.

Marks 03

- (a) Explain Standard Test Signals used in control system. 0.1
 - **(b)** What are the limitations of open-loop systems over closed-loop systems? 04 List the advantages of closed-loop system over open-loop system.

(c) 07 Determine the overall transfer function $\frac{C}{R}$ for the system whose block diagram is shown in fig. below using block diagram reduction technique.



- (a) Define the following: (1) Rise time (2) Delay time (3) Settling time. 0.2 03
 - **(b)** Obtain the transfer function $\frac{X_1(s)}{F(s)}$ and $\frac{X_2(s)}{F(s)}$ of the mechanical system shown in fig. below.



07

04

(c) For the unity feedback control system with $G(s) = \frac{\kappa}{s(s+1)(s+2)}$. Find the

range of K for system that will cause the system to be stable, marginally stable and unstable. Make suitable comments.

- OR
- Determine the stability of the system represented by the characteristic 07 (c) equation $s^{6} + 3s^{5} + 5s^{4} + 9s^{3} + 8s^{2} + 6s + 4 = 0$ by means of the Routh criterion. Determine the number of roots of the characteristic equation lying in the right-half of s-plane.

- 03 **O.3** (a) Explain the terms with respect to root locus. (i) centroid (ii) angle of arrival and angle of departure (iii) breakaway and break in points.
 - **(b)** State and explain nyquist stability criteria.
 - 07 (c) Sketch bode plot showing the magnitude in decibels and phase angle in degrees as a function of log frequency for the transfer function given below. Determine the gain cross over frequency.

$$G(s) = \frac{10}{s(1+0.5s)(1+0.01s)}$$
OR

- Q.3 (a) Describe the steps to construct the polar plot.
 - Explain relationship between time and frequency response. 04 **(b)**
 - Consider a unity feedback control system with an open-loop transfer function. (c) 07

$$G(s)H(s) = \frac{K(s+1)(s+2)}{(s+0.1)(s-1)}$$

Draw the root locus of the system with the gain K as a variable. Find from the root locus plot, the value of gain K for which a closed-loop system is critically damped.

- 0.4 **(a)** Explain the effect of integral control action on system Performance. 03
 - What is compensation? What are the different types of compensations? 04 **(b)**
 - (c) Draw the bode plot for phase-lead network and derive expression for the 07 parameter α in terms of $\Phi_{\rm m}$.

OR

Q.4	(a)	State limitations and effects of Lag compensator.	03
	(b)	State the limitations of a single stage phase lead compensation.	04

- Explain step by step Procedure for Phase Lag Network. 07 (c)
- Explain the advantages of bode plot. Q.5 (a)
 - How will you define controllability and observability of the system? 04 **(b)**
 - (c) Draw a series RLC circuit. Obtain its state space model considering current 07 and capacitor voltage as state variables.

OR

- Define the following terms: Gain margin, phase margin, bandwidth, resonant 03 Q.5 **(a)** peak
 - Explain the following terms: (i) State (ii) State Variables 04 **(b)** (iii) State Space (iv) State transition matrix
 - A linear time-invariant system is described by the following state variable 07 (c) model:

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & -2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$$
$$y(t) = \begin{bmatrix} 1 & 2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

Comment on the controllability and observability of the system.

04

03

03